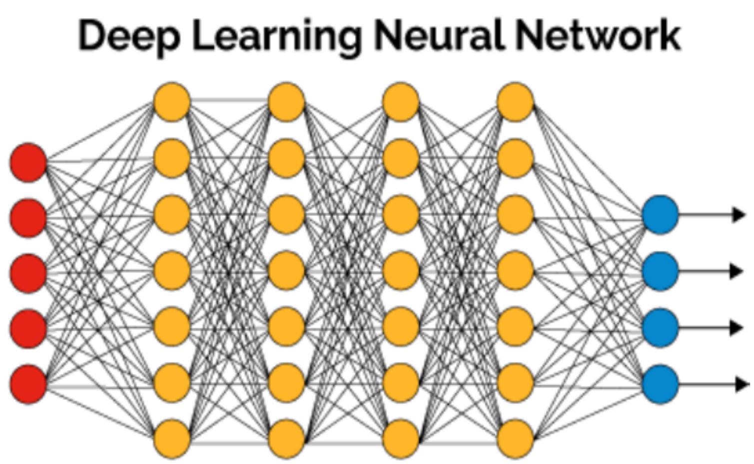
# Statistical Physics and Machine Learning

Machine learning is a fascinating subject both from the theoretical and practical point of view. Although deep neural networks were introduced decades ago, only recently their implementation became possible thanks to an increased computational power combined with a huge amount of data (used as learning set). This lead to a real revolution that is still bursting right now [1]. Almost every day a new ground-breaking application of machine learning--thought to be impossible just a few years ago--comes out. Despite their success, the theoretical understanding of deep neural networks is quite poor. Practitioners have developed recipes to construct and train them but fundamental questions remain opened. Answering them not only has the potentiality of leading to great improvements as well as avoiding dramatic pitfalls but it is a fascinating scientific subject at the boundary between high-dimensional statistics, theoretical physics, mathematics and computer science. The aim of this project is to theoretically analyze deep neural networks by studying simplified models that retain the essential ingredients and that are amenable to a full theoretical analysis.

In a nutshell deep neural networks use a very non-linear function of a very large number (e.g. $10^8$) of variables, called weights, to learn from a very large (e.g. $10^9$) number of data. A standard example is image recognition. The learning process is performed by minimizing a loss function: one has to find the weights such that the sum over the learning data set of the prediction errors is minimized.




*Example of an artificial neural network with four hidden layers in yellow, one input layer in red and one output layer in blue.*

The problem encountered in the learning process of a deep neural network has very strong similarity with problems central in statistical physics. The loss function is very much like an energy function of a disordered system: the quenched disorder is encoded in the learning data set, the degrees of freedom are the weights, the learning process is like finding the global minimum of the energy landscape.

The aim of this project is to understand the dynamics associated to the training of neural networks, and the mechanisms that make learning possible for over-parametrized networks.

We will follow a twofold approach that will combine analytics and numerics. We will study simplified models in order to develop an analytical theory of many phenomena observed in practice. Concomitantly, we will perform numerical experiments on realistic deep neural networks in order to gain more insights and test analytical predictions found in simplified models.

The internship and PhD are for theoretically oriented students with a very good basis in statistical physics and taste for coding.

The student will be involved in the activities of the Paris Research Institute on Artificial Intelligence (PRAIRIE) and the future data science center at ENS.

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[1] *Deep Learning* Y. LeCun, Y. Bengio, G. Hinton Nature 521 (2015).

Some references representative of G. Biroli's research work on Machine Learning

Baity-Jesi, Marco, et al. "Comparing dynamics: Deep neural networks versus glassy systems." *arXiv preprint arXiv:1803.06969* (2018), ICML 2018.
d'Ascoli, Stéphane, et al. "Finding the Needle in the Haystack with Convolutions: on the benefits of architectural bias." *arXiv preprint arXiv:1906.06766, Advances in Neural Information Processing Systems*. 2019.
Geiger, Mario, et al. "Scaling description of generalization with number of parameters in deep learning." *arXiv preprint arXiv:1901.01608* (2019).
Mannelli, Stefano Sarao, et al. "Who is Afraid of Big Bad Minima? Analysis of gradient-flow in spiked matrix-tensor models." *arXiv preprint arXiv:1907.08226, Advances in Neural Information Processing Systems*. 2019.